$\qquad$
Here's a picture of all of the rectangles that enclose 12 squares.


Notice that it doesn't matter which direction the rectangles are facing. A 1 by 12 rectangle has the same dimensions as a 12 by 1 rectangle. If we cut them out, we could easily rotate them.

If I make a list of the different rectangles using 12 squares I would have:

| 12 |
| :---: |
| $1 \times 6$ |
| $2 \times 6$ |

$3 \times 4$

I could keep going, but the second half of the list is just a repeat of the rectangles in the first half of the list.

We would say that the factors of 12 are $1,2,3,4,6$, and 12 .
One way to think about this is that $1,2,3,4,6$, and 12 are the dimensions of all of the possible rectangles we can make with 12 squares.

12
$1 \times 12$
$2 \times 6$
$3 \times 4$
$4 \times 3$
$6 \times 2$
$12 \times 1$

Sketch all of the rectangles that can enclose 16 squares.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
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Did you get three rectangles? You should have a $1 \times 16$, a $2 \times 8$ and a $4 \times 4$ rectangle. Remember that squares are just special rectangles where all four sides are the same length.

List the factors of 16 . When listing factors, please list them from smallest to largest.

Complete the chart. You can draw rectangles if it is helpful.

| Number | Factors | How many <br> factor are there? |
| :---: | :--- | :---: |
| 1 | 1 | 1 |
| 2 | 1,2 | 2 |
| 3 |  |  |
| 4 |  |  |
| 5 |  |  |
| 6 |  |  |
| 7 |  |  |
| 8 |  |  |
| 9 |  |  |
| 10 |  |  |
| 11 |  |  |
| 12 | $1,2,3,4,6,12$ | 5 |
| 13 |  |  |
| 14 |  |  |
| 15 |  |  |
| 16 | $1,2,4,8,16$ |  |
| 17 |  |  |
| 18 |  |  |
| 19 |  |  |
| 20 |  |  |

Which numbers have exactly 2 factors? List them.

Now list the factors of 72 .

Chances are that you don't want to draw all of rectangles first. Plus, not having a systematic method will probably result in missing some factors. Did you get all 12 factors?

It is time to add some more tools to your mathematical tool kit to make a task like this more manageable.

